

10/08/2015

Econ 142 Discussion Week 7 Assignment Answer Key

1) $Q_D = 240 - 4P$
 $Q_S = 2P$

Equilibrium Price & Quantity:

At Eq. $Q_D = Q_S$. You can find eq. P by setting the equations for Q_D & Q_S equal to one another, and then solving for P :

$$240 - 4P = 2P$$

$$240 = 6P$$

$$240/6 = P$$

$$P = 40$$

The plug the eq P into either the Q_S or Q_D equation to get the eq Q :

$$\begin{aligned} Q_S &= 2P \\ &= 2(40) \\ &= 80 \end{aligned}$$

$$\begin{aligned} Q_D &= 240 - 4(40) \\ &= 240 - 160 \\ &= 80 \end{aligned}$$

So $Q = 80$

1) continued

Price Elasticity of Demand =

$$\epsilon = \frac{dQ_D}{dP} \cdot \frac{P}{Q}$$

$$\frac{dQ_D}{dP} = -4 \quad \text{and} \quad \frac{P}{Q} = \frac{40}{80} = .5$$

$$\text{So } \epsilon = -4 \cdot (.5) = \boxed{-2} \quad (\text{elastic})$$

Price Elasticity of Supply:

$$\epsilon = \frac{dQ_S}{dP} \cdot \frac{P}{Q}$$

$$\frac{dQ_S}{dP} = 2 \quad \text{and} \quad \frac{P}{Q} = .5$$

$$\text{So } \epsilon = 2 \cdot (.5) = \boxed{1}$$

Impact of Price Increase on Total Revenue:

Increase in price will decrease total revenue because demand is elastic.

$$2) \quad Q_D = 100 - \frac{1}{2}P$$

$$Q_S = 2P$$

Equilibrium Price & Quantity:

$$\begin{array}{l}
 Q_D = Q_S \\
 100 - \frac{1}{2}P = 2P \\
 100 = 2.5P \\
 100/2.5 = P \\
 \boxed{P = 40}
 \end{array}
 \quad \left. \vphantom{\begin{array}{l} Q_D = Q_S \\ 100 - \frac{1}{2}P = 2P \\ 100 = 2.5P \\ 100/2.5 = P \\ \boxed{P = 40} \end{array}} \right\}
 \begin{array}{l}
 Q_D = 100 - \frac{1}{2}(40) \\
 = 100 - 20 \\
 = 80 \\
 \boxed{Q = 80}
 \end{array}
 \quad \begin{array}{l}
 Q_S = 2(40) \\
 = 80
 \end{array}$$

Price Elasticity of Demand:

$$E = \frac{dQ_D}{dP} \cdot \frac{P}{Q} = -\frac{1}{2} \cdot \frac{40}{80} = \boxed{-.25}$$

~~inelastic~~ inelastic

Price Elasticity of Supply:

$$E = \frac{dQ_S}{dP} \cdot \frac{P}{Q} = 2 \cdot \frac{40}{80} = \boxed{1}$$

Unit elastic

Price Changes & Revenue:

Increasing price would increase revenue because demand is inelastic. Decreasing price would decrease revenue.

3. Calculate price elasticity of demand based using the following table of values:

	Price	Quantity
Point A	\$3.50	2,000
Point B	\$3.30	2,100

$$\epsilon = \frac{\Delta Q / \bar{Q}}{\Delta P / \bar{P}}$$

$$\Delta Q = 2000 - 2100 = -100$$

$$\bar{Q} = \frac{2000 + 2100}{2} = 2050$$

$$\Delta P = 3.50 - 3.30 = .20$$

$$\bar{P} = \frac{3.50 + 3.30}{2} = \frac{6.8}{2} = 3.4$$

$$\epsilon = \frac{-100 / 2050}{.20 / 3.4}$$

$$= \frac{-.0488}{.0588} = \boxed{-.83}$$

Is demand elastic or inelastic between point A and point B?

It is inelastic because ~~there~~ ϵ is less than 1 in absolute value.

If the quantity at point B were 2,500, what would the price elasticity of demand be? Is demand elastic or inelastic in this case?

$$\Delta Q = 2000 - 2500 = -500$$

$$\bar{Q} = \frac{2000 + 2500}{2} = \frac{4500}{2} = 2250$$

$$\Delta P = .20$$

$$\bar{P} = 3.4 \quad \left. \begin{array}{l} \Delta P = .20 \\ \bar{P} = 3.4 \end{array} \right\} \text{same as above}$$

$$\epsilon = \frac{\Delta Q / \bar{Q}}{\Delta P / \bar{P}} = \frac{-500 / 2250}{.0588}$$

$$= \frac{-.222}{.0588}$$

$$= \boxed{-3.78}$$

In this case the demand is elastic.