## ECON 522

Sept. 18, 2017

## Money and Inflation

- From Chapter 4, can skip parts on:
- "Bank Capital, Leverage, and Capital Requirements" in Section 4.2
- "A Model of the Money Supply" in Section 4.3 (start with "The Instruments of Monetary Policy" for that section)
- Today: Chapter 5, long-run theory of inflation. From the book, can skip:
- Sections 5.4 to 5.6


## Velocity

- Velocity of money = the number of times the average dollar bill changes hands in a given time period; (the rate at which money circulates)
- Example: If in 2015 there were $\$ 500$ billion in transactions and the money supply was $\$ 100$ billion, then the average dollar was used in 5 transactions. Each dollar would have had to been used on average that many times.
- Equation:

Velocity (V) = Value of all Transactions (T) / Money Supply (M)

- Use nominal GDP as a proxy for total transactions ( $\mathrm{T} \sim=\mathrm{P} \times \mathrm{Y}$ )
$\mathrm{V}=(\mathrm{P} \times \mathrm{Y}) / \mathrm{M}$
- Difference between nominal GDP and total value of transactions?


## Quantity Equation

- Rearranging the velocity equation from the prior slide gives:
$M \times V=P \times Y$
- Associated w the Quantity Theory of Money (idea that changes in quantity of money lead to changes in nominal expenditure)


## Money Demand

- $M / P=$ real money balances $=$ the purchasing power of the money supply
- Note, this is similar to other cases where we divide by P to look at variables in "real" terms
- Money Demand Function: $(M / P)^{\wedge} d=L(i, Y)$
- Ignoring i for the moment: we can write money demand as $(M / P)^{\wedge} d=k Y$
- Where $k$ is how much money people wish to hold for each dollar of income
- This connects money demand to the quantity equation: $k=1 / \mathrm{V}$
- When $k$ is large, people hold lots of money relative to their incomes, and $V$ is small, meaning money changes hands infrequently


## Quantity Theory of Money

- From the Quantity Equation, assume V is exogenously determined and constant (not changing)
- Then, money supply (M) determines nominal GDP (P x Y) ....
- Real GDP $(\mathrm{Y})$ is still determined by K , $L$ and technology ... Introducing more money into the economy shouldnt change how much people are able to produce
- Price level $(P)=$ nominal GDP $(P \times Y) /$ real GDP $(Y)$
- Similar to the way we define the GDP deflator


## Quantity Theory in Growth Rates

- Math Rule: the growth rate of a product ( $a \times b$ ) equals the sum of the growth rates:
- Growth rate ( $a \times b$ ) = growth rate (a) + growth rate (b)
- Write out the quantity equation in terms of growth rates
- Growth rate of V is 0 by assumption (we assumed V is not changing)
- Growth rate of $\mathrm{P}=$ inflation rate
- Solve for inflation rate, and you get that the inflation rate equals the difference in the growth rate of the money supply and the growth rate of real GDP
- Interpretation: Normal economic growth requires a certain amount of money supply growth to facilitate growth in transactions. Money growth in excess of that amount leads to inflation.


## Example

- If real GDP is growing by $3 \%$ per year over the long run, what rate of money supply growth would the central bank need to target to achieve zero inflation (on average over the long run)?


## QTM Prediction

- Growth in Y (real GDP) depends on factors of production and technological progress. We take those as fixed (given outside the model) for now.
- The QTM predicts a one-for-one relation between changes in the money growth rate and changes in the inflation rate. A change in this money growth rate, under this theory, should cause an equal change in the inflation rate.
- In data, countries with higher money growth rates do tend to have higher inflation rates.



## Example

Suppose $V$ is constant, $M$ is growing at $5 \%$ per year, $Y$ is growing at $2 \%$ per year, and $r=4$.

- Solve for i.
- If the Fed increases the money growth rate by 2 percentage points, what is the change in i .
- If the growth rate of $Y$ falls to $1 \%$ per year, what happens to the inflation rate? What would the Fed need to do to keep the inflation rate constant?


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